



Isfahan University of Technology

Amirkabir University of Technology
(Tehran Polytechnic)



Zinc-Smelter Logistics Network Design under Interruption Risks

Pooya Hoseinpour

Assistant Professor, Industrial Engineering and Management Systems,
Amirkabir University of Technology (Tehran Polytechnic), Iran

Isfahan University of Technology

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Outline



- Zinc-smelting industry
- Zinc-mining logistics
- Interruptions in zinc-smelters
- Problem modeling
- Solution algorithm
- Managerial insights
- Conclusion and extensions

Zinc-smelting industry



- One of the industries that is extremely capital-intensive!

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- Zinc-smelting is the process of converting zinc concentrates (ores that contain zinc) into zinc ingots.

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Smelting Process



Zinc-smelting industry



zinc-smelting process

- There are basically two common methods for producing zinc ingots:
pyrometallurgical and **hydrometallurgical**.

Zinc-smelting industry



zinc-smelting process

- There are basically two common methods for producing zinc ingots:
 pyrometallurgical and **hydrometallurgical**.
- Four main steps:
 - Roasting
 - Leaching and purification
 - Electrolysis
 - Smelting and casting

Zinc-smelting industry

zinc-smelting process



Transporting zinc concentrates to
the temporary storage



Zinc-smelting industry

zinc-smelting process



Transporting zinc concentrates to the temporary storage



Transporting the mixed concentrates to the roasters



Zinc-smelting industry

zinc-smelting process



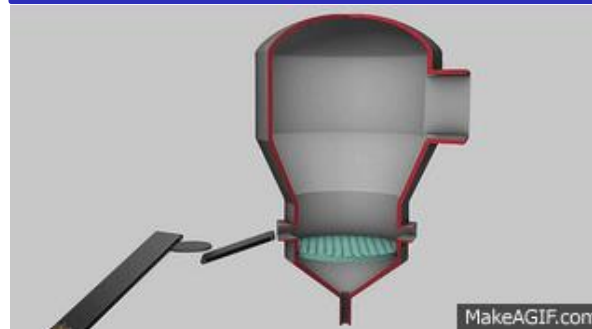
Transporting zinc concentrates to the temporary storage



Transporting the mixed concentrates to the roasters



Roasting plant: convert zinc sulfide to impure zinc oxide



Zinc-smelting industry

zinc-smelting process



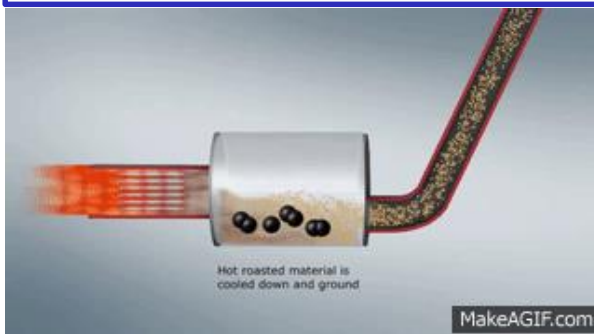
Transporting zinc concentrates to the temporary storage



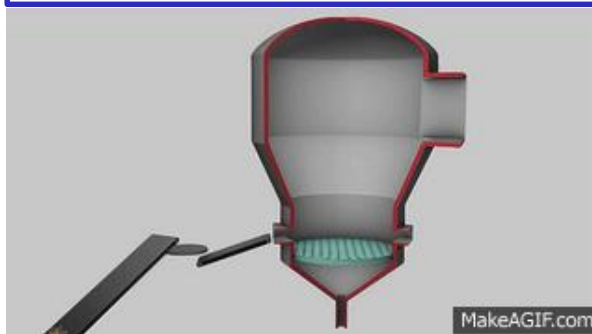
Transporting the mixed concentrates to the roasters



Transporting zinc oxide to the leaching plant



Roasting plant: convert zinc sulfide to impure zinc oxide

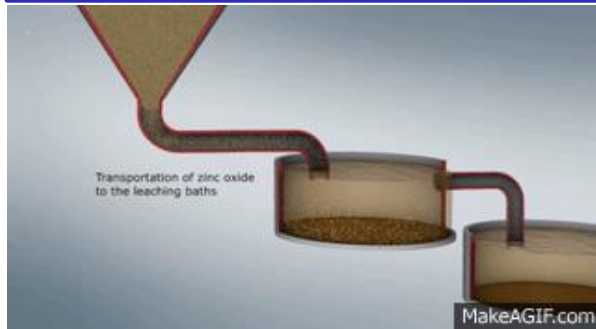


Zinc-smelting industry

zinc-smelting process



Leaching process: impurities are precipitated

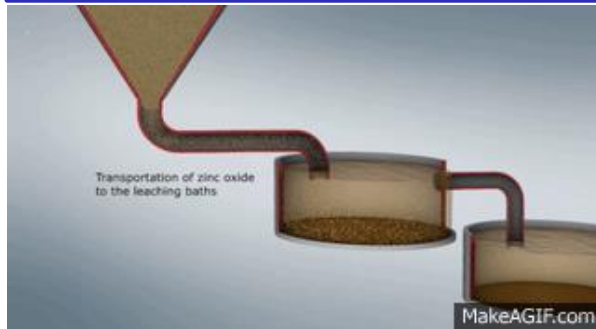


Zinc-smelting industry

zinc-smelting process



Leaching process: impurities are precipitated



Transporting roasted materials to the Electrolysis plants

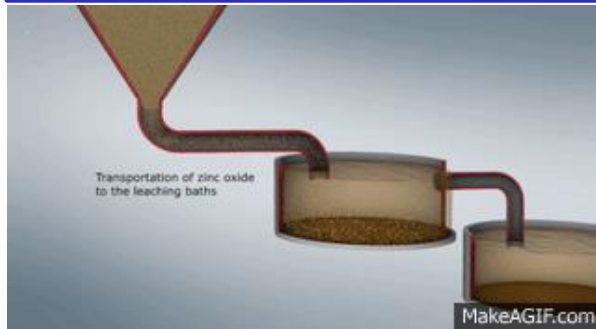


Zinc-smelting industry

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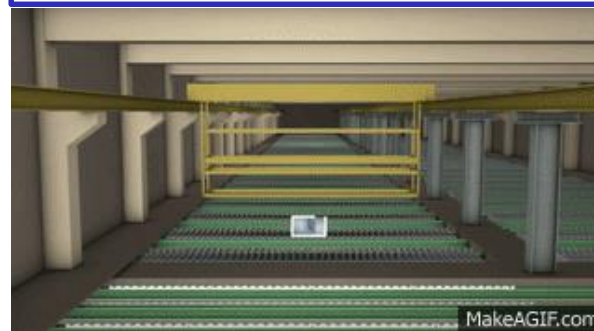
Leaching process: impurities are precipitated



Transporting roasted materials to the Electrolysis plants



Electrolysis process: zinc is deposited in Aluminum sheets

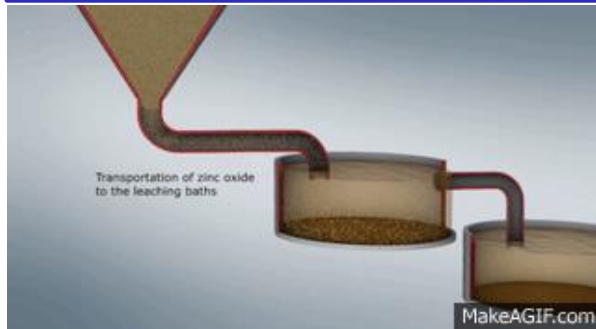


Zinc-smelting industry

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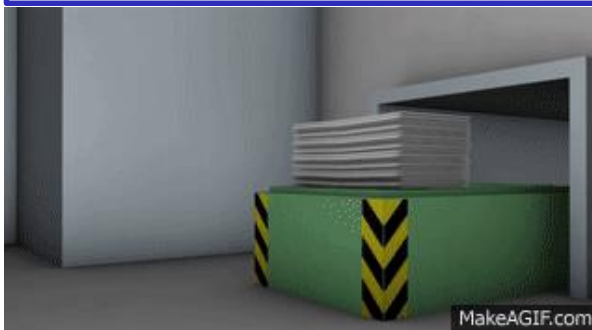
Leaching process: impurities are precipitated



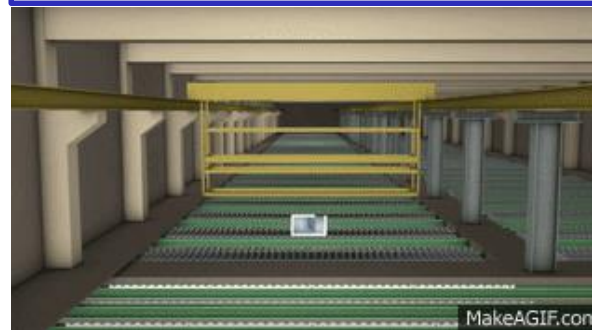
Transporting roasted materials to the Electrolysis plants



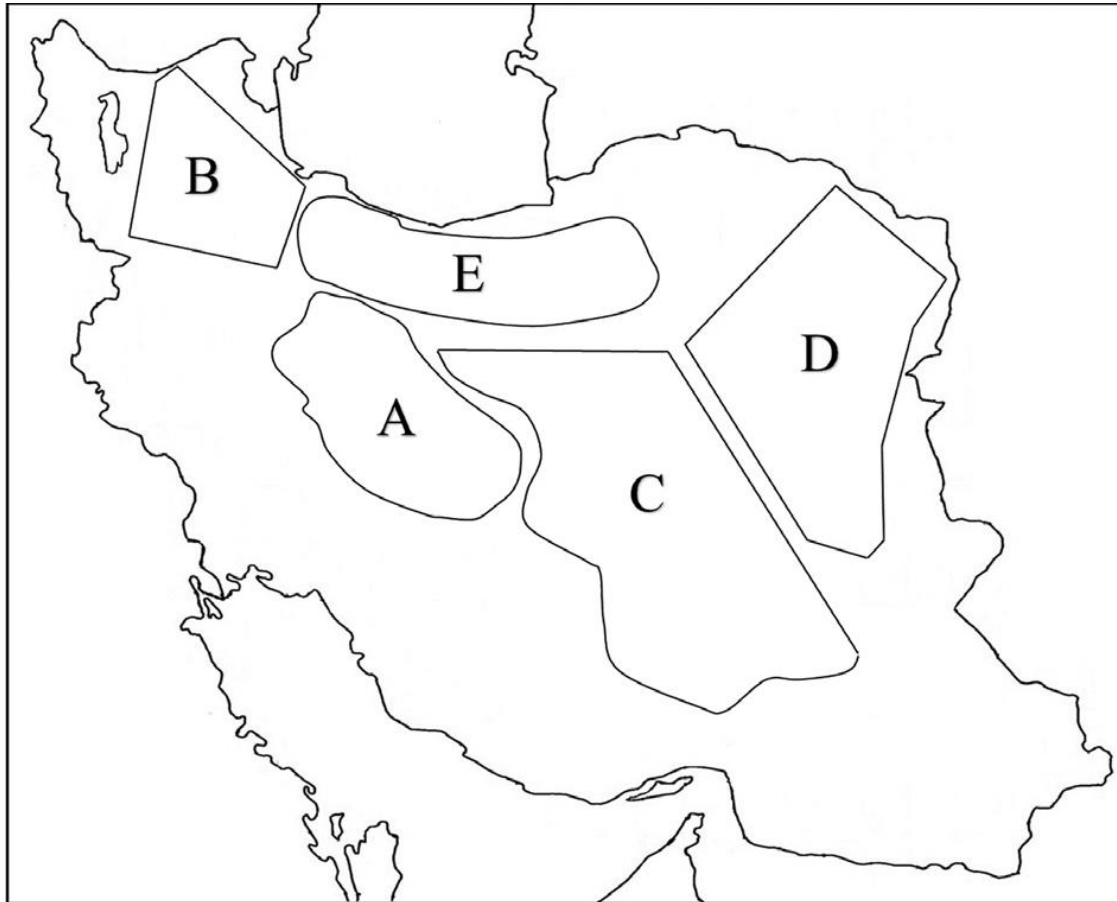
Melting and casting process; done in induction furnaces



Electrolysis process: zinc is deposited in Aluminum sheets



Zinc-mining logistics



Iran Zinc Mines Development Company plans to increase zinc production, i.e., zinc ingots, by making investments to establish new smelters.

Areas of zinc mineralization can be classified into five regions.

Two potential places are selected from each region as candidate locations for new smelters.

Zinc-mining logistics



- Zinc-mining logistics is concerned with the optimal **number, location, and service capacity** of smelters, as well as, **allocation** of zinc mines.

Zinc-mining logistics



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- Cost-effectively delivering the zinc ingots to the market is the main goal of mining ventures.

Zinc-mining logistics



- Zinc-mining logistics is concerned with the optimal **number, location, and service capacity** of smelters, as well as, **allocation** of zinc mines.
- Cost-effectively delivering the zinc ingots to the market is the main goal of mining ventures.
- Cost includes: smelters' establishing fixed cost, production (service) cost, transportation cost, and storage (congestion) cost.

Interruptions in zinc-smelters



Smelting process of each smelter can be stopped frequently due to different kinds of interruptions in any plants:

Interruptions in zinc-smelters



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power outage

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(e.g. fuel, sulfuric acid and water for leaching process)

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unscheduled machine breakdowns

(e.g. improper maintenance or use, and warning signals)

Interruptions in zinc-smelters



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personnel/operating errors

Interruptions in zinc-smelters



Smelting process of each smelter can be stopped frequently due to different kinds of interruptions in any plants:

Facility Location Problem with Stochastic Demands and Congestion (Service system design problem) with service interruptions

(e.g. fuel, sulfuric acid and water for leaching process)

unscheduled machine breakdowns

(e.g. improper maintenance or use, and warning signals)

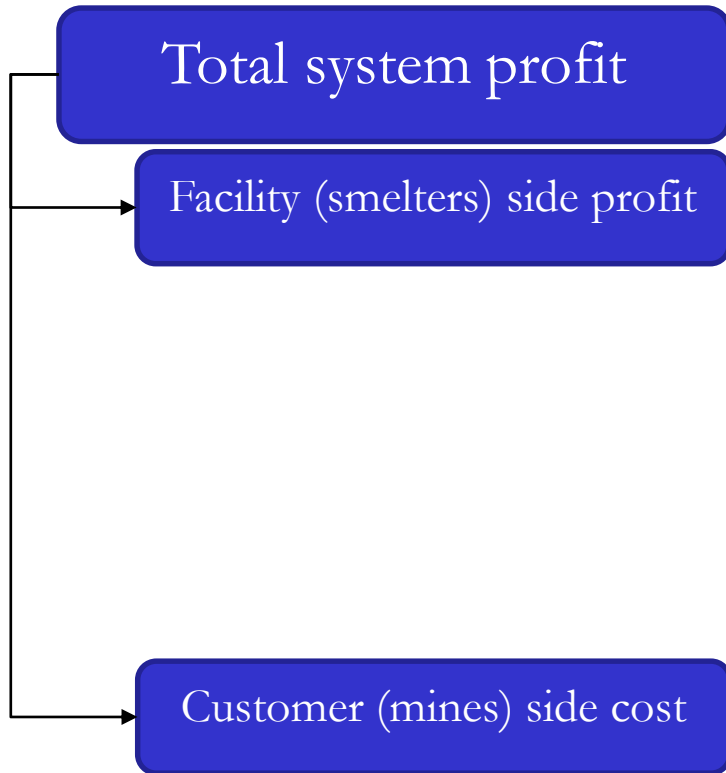
personnel/operating errors

Problem modeling

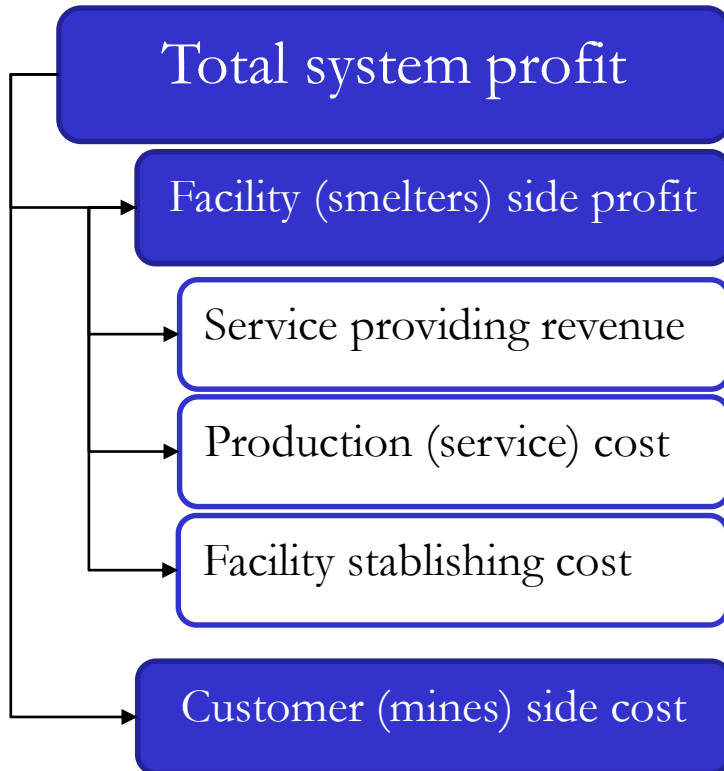


Total system profit

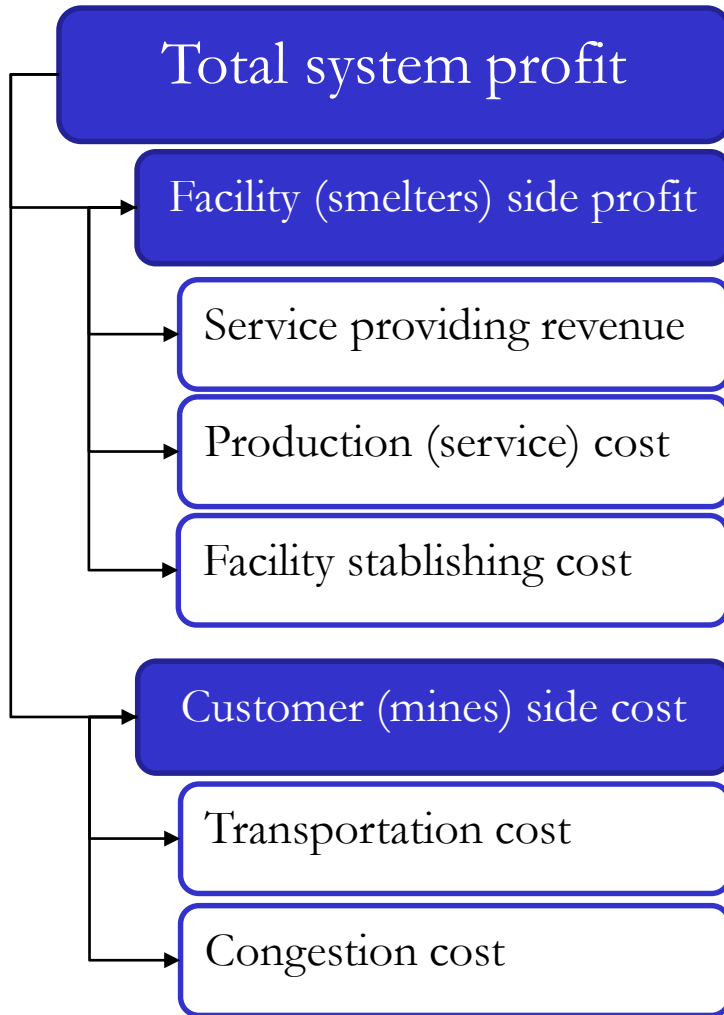
Problem modeling



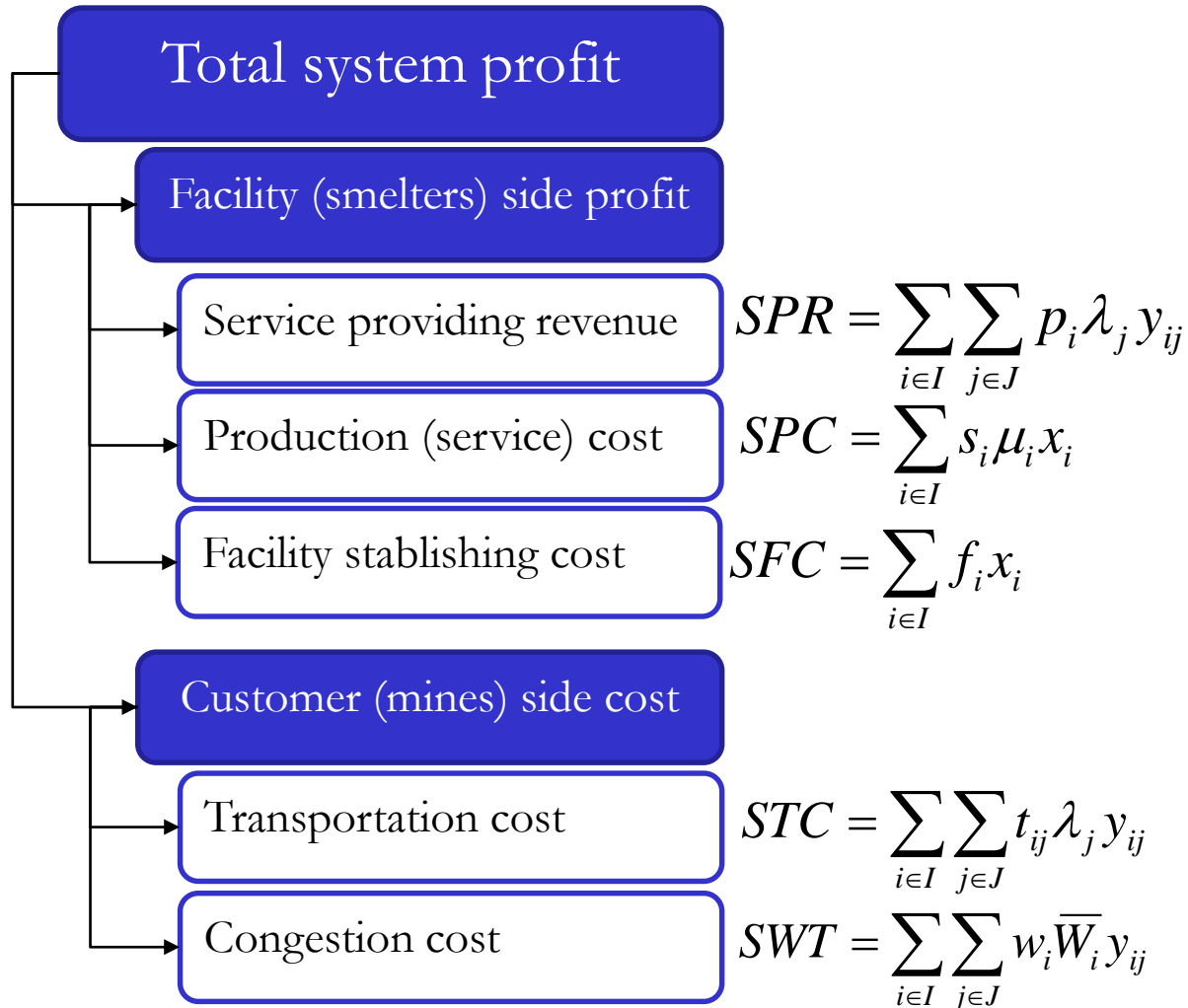
Problem modeling



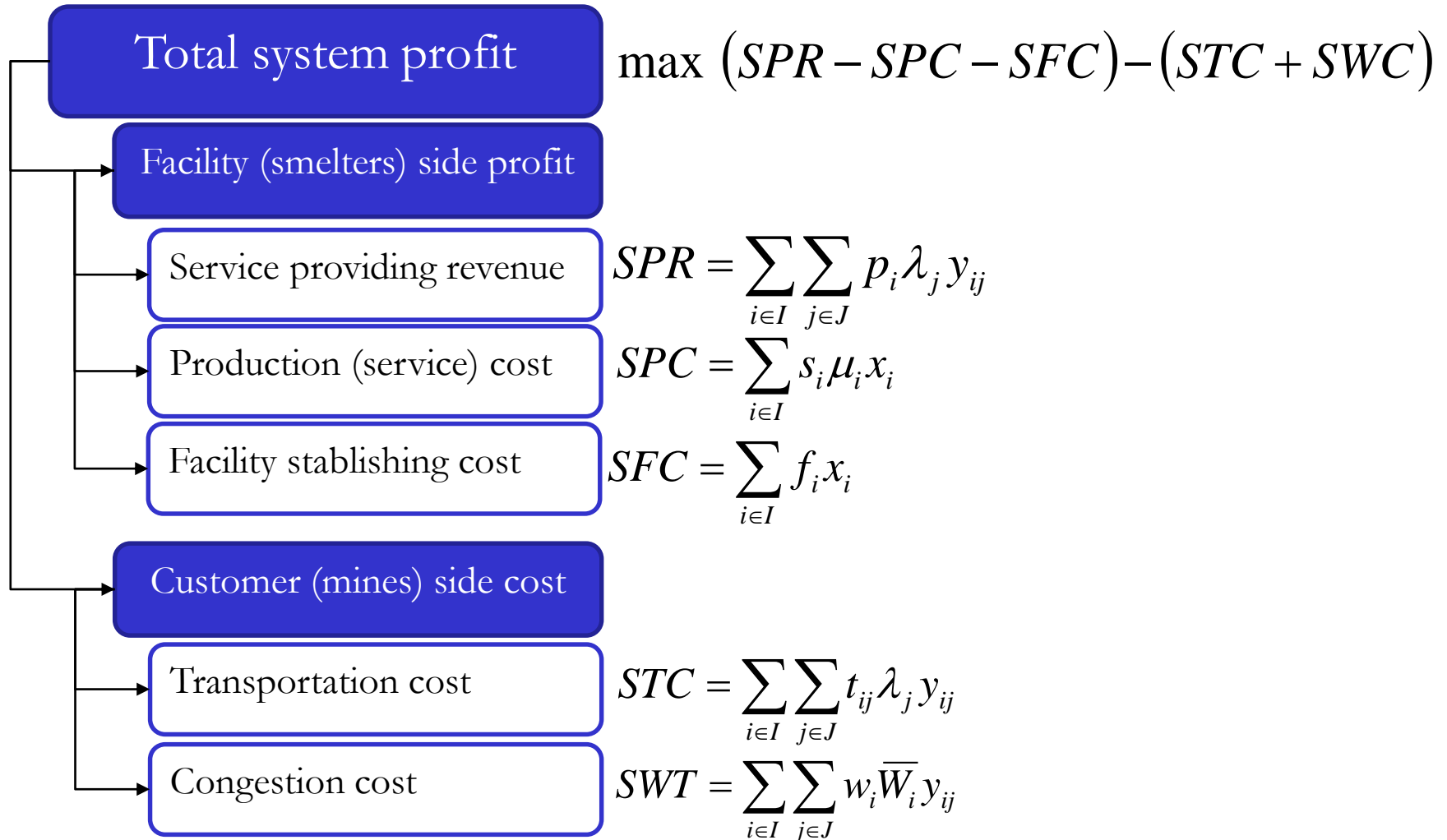
Problem modeling



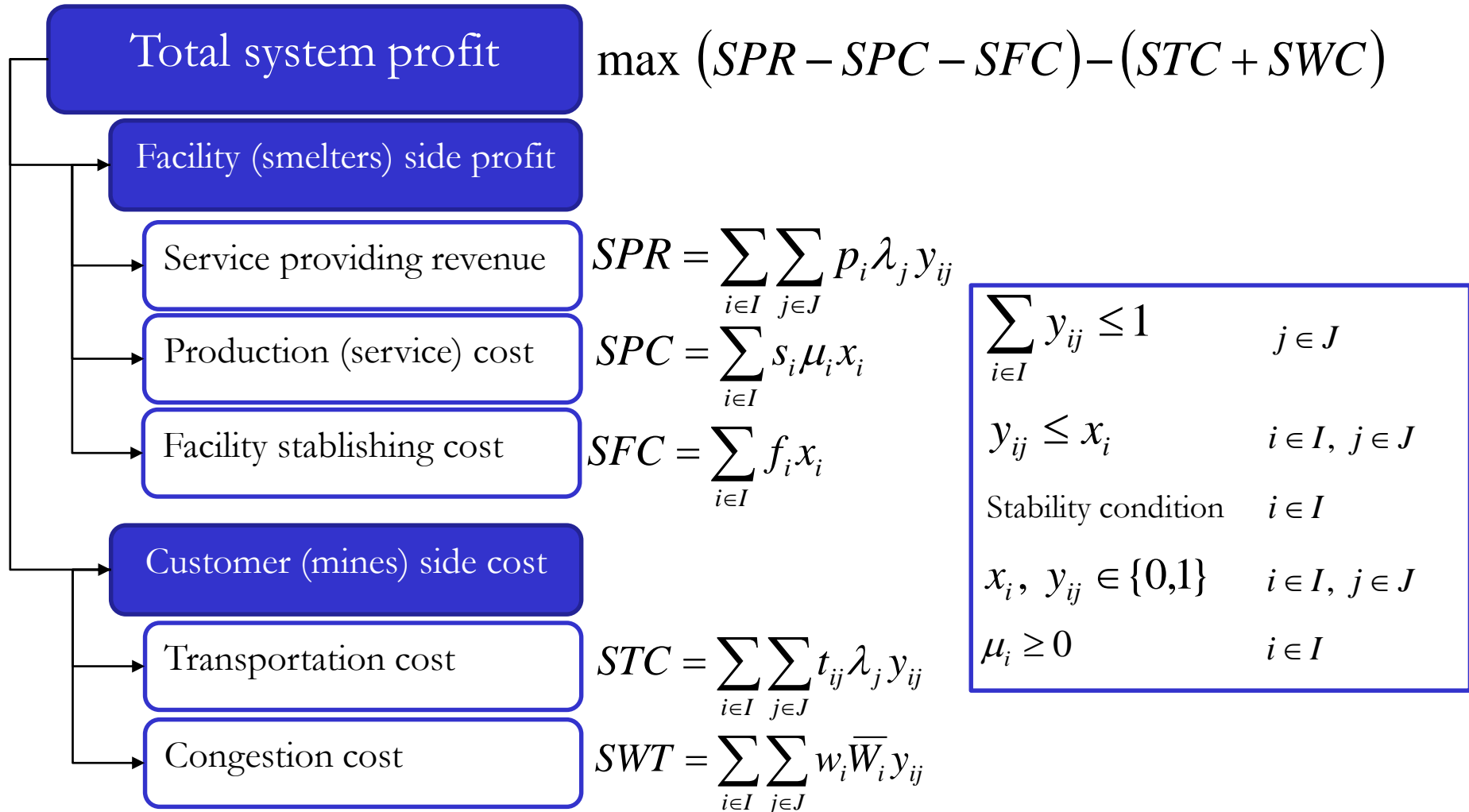
Problem modeling



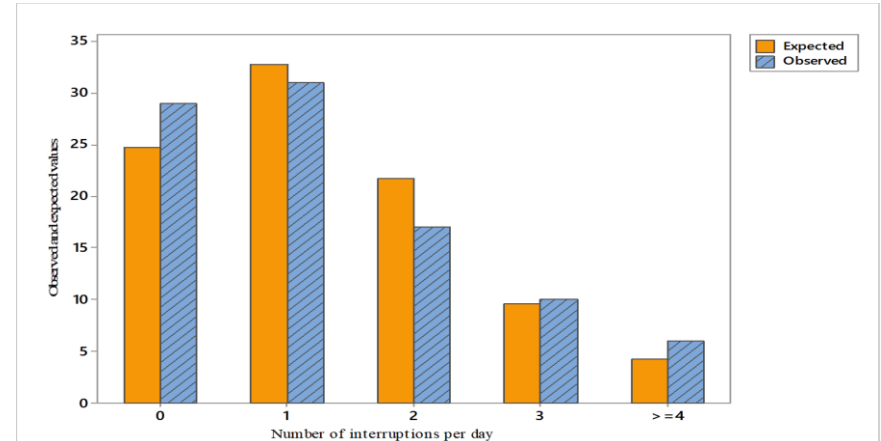
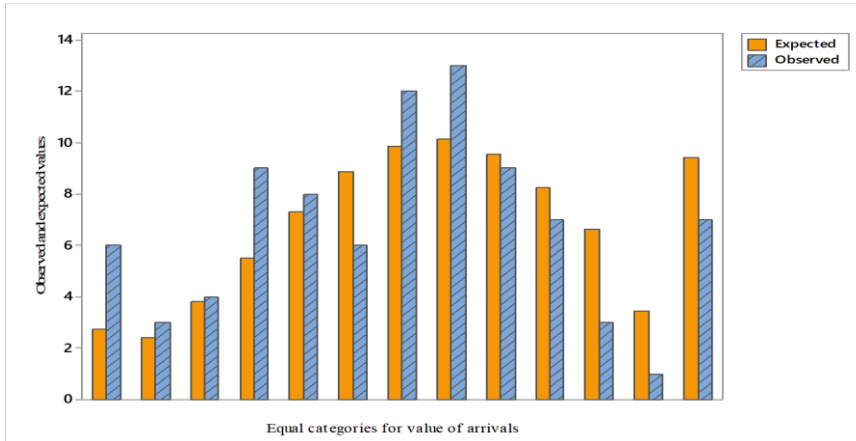
Problem modeling



Problem modeling

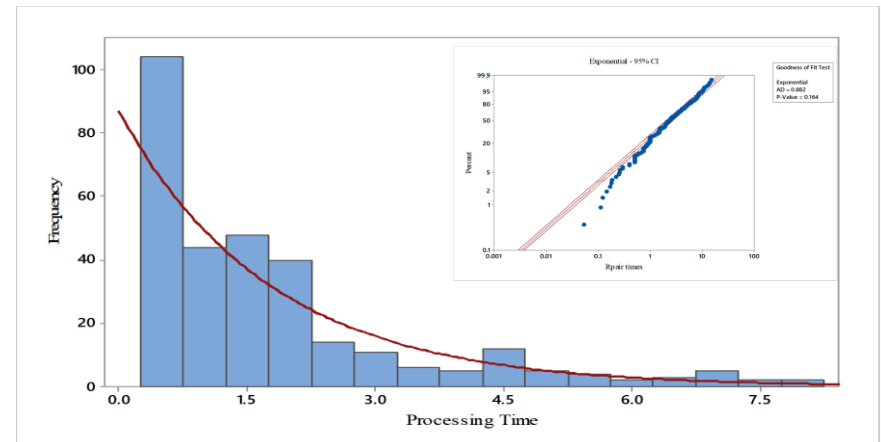
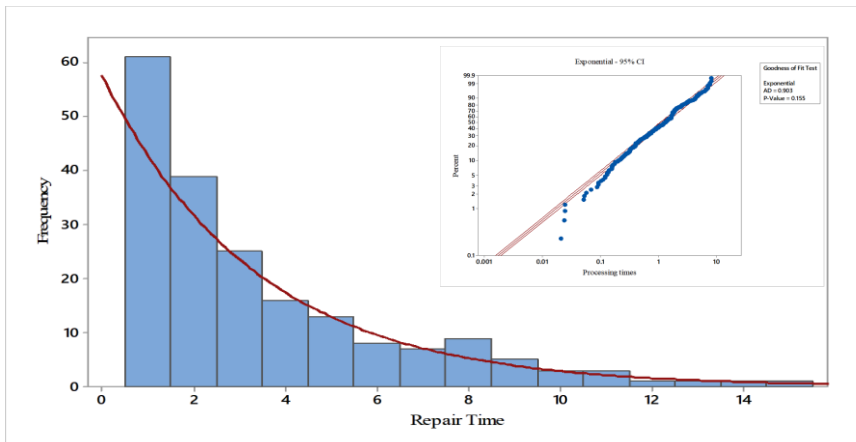


Problem modeling



a) H: arrivals follow a Poisson process, number of arrivals per time has a Poisson distribution; $p_v = 0.293$.

b) H: Interruptions follow a Poisson process, number of interruptions per time has a Poisson distribution; $p_v = 0.459$.



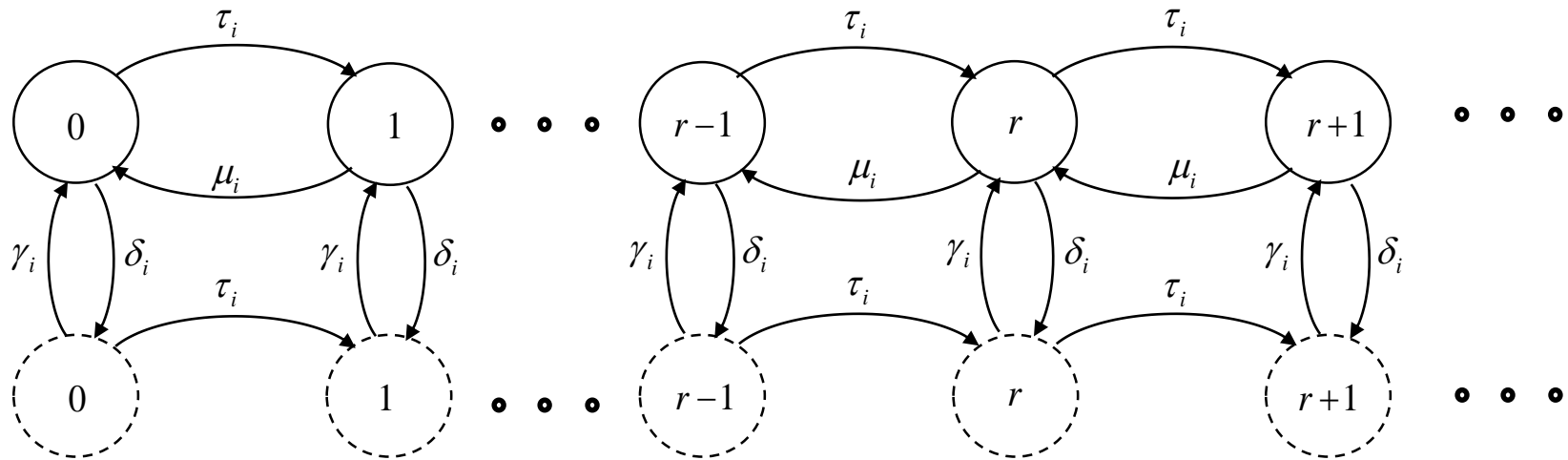
c) H: Processing times are exponentially distributed; $p_v = 0.155$.

d) H: Repair times are exponentially distributed; $p_v = 0.164$.

Problem modeling



$$\tau_i = \sum_{j \in J_i} \lambda_{ij}$$



Interruption rate

δ_i

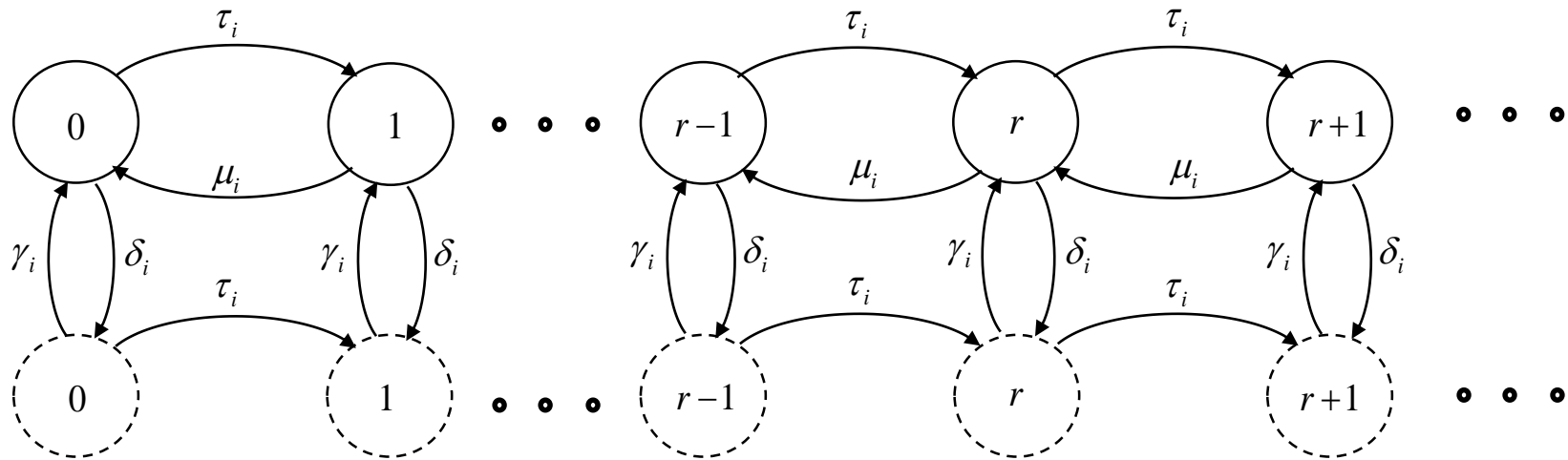
Recovery rate

γ_i

Problem modeling



$$\tau_i = \sum_{j \in J_i} \lambda_{ij}$$



$$G_i(z) = \frac{((\mu_i - \tau_i)\gamma_i - \tau_i\delta_i)(\delta_i + \tau_i(1-z) + \gamma_i)}{(\delta_i + \gamma_i)((\tau_i(1-z) + \gamma_i)(\mu_i - \tau_i z) - \tau_i\delta_i z)} \quad |z| \leq 1 \quad \gamma_i\mu_i > (\delta_i + \gamma_i)\tau_i$$

$$\bar{W}_i = \frac{(\delta_i + \gamma_i)^2 + \mu_i\delta_i}{(\delta_i + \gamma_i)(\gamma_i(\mu_i - \tau_i) - \tau_i\delta_i)}$$

Interruption rate

δ_i

Recovery rate

γ_i

Problem modeling



$$\max_{\mathbf{x}, \boldsymbol{\mu}, \mathbf{y}} \quad v(\mathbf{x}, \boldsymbol{\mu}, \mathbf{y}) = \sum_{i \in I} \sum_{j \in J} p_i \lambda_{ij} y_{ij} - \sum_{i \in I} f_i x_i - \sum_{i \in I} s_i \mu_i x_i - \sum_{i \in I} \sum_{j \in J} t_{ij} \lambda_{ij} V_{ij}$$

$$- \sum_{i \in I} \frac{w_i \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \left((\delta_i + \gamma_i)^2 + \delta_i \mu_i \right)}{(\delta_i + \gamma_i) \left(\gamma_i \mu_i - (\delta_i + \gamma_i) \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \right)}$$

s.t.

$$\sum_{i \in I} y_{ij} \leq 1 \quad j \in J$$

$$y_{ij} \leq x_i \quad i \in I, j \in J$$

$$\sum_{j \in J} \lambda_j y_{ij} < \frac{\gamma_i}{\delta_i + \gamma_i} \mu_i \quad i \in I$$

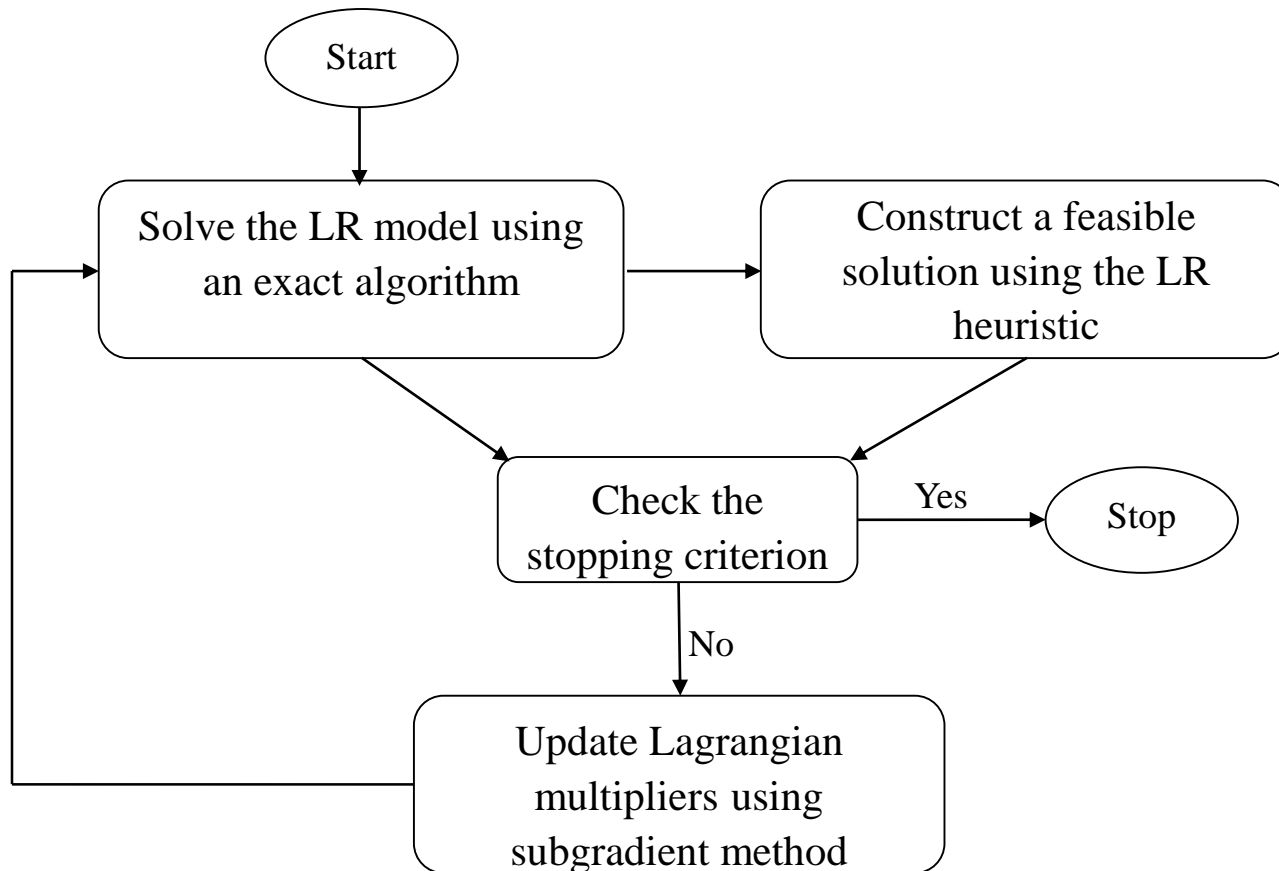
$$\mu_i \geq 0 \quad i \in I$$

$$y_{ij} \in \{0,1\} \quad i \in I, j \in J$$

$$x_i \in \{0,1\} \quad i \in I$$

Solution algorithm

Lagrangian Relaxation



Solution algorithm



$$\max_{x, \mu, y} \quad v(x, \mu, y) = \sum_{i \in I} \sum_{j \in J} p_i \lambda_{ij} y_{ij} - \sum_{i \in I} f_i x_i - \sum_{i \in I} s_i \mu_i x_i - \sum_{i \in I} \sum_{j \in J} t_{ij} \lambda_{ij} V_{ij}$$

$$- \sum_{i \in I} \frac{w_i \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \left((\delta_i + \gamma_i)^2 + \delta_i \mu_i \right)}{(\delta_i + \gamma_i) \left(\gamma_i \mu_i - (\delta_i + \gamma_i) \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \right)}$$

$$\text{s.t.} \quad \sum_{i \in I} y_{ij} \leq 1 \quad j \in J$$

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$$\mu_i \geq 0 \quad i \in I$$

$$y_{ij} \in \{0,1\} \quad i \in I, j \in J$$

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Solution algorithm



$$\max_{x, \mu, y} \quad v(x, \mu, y) = \sum_{i \in I} \sum_{j \in J} p_i \lambda_{ij} y_{ij} - \sum_{i \in I} f_i x_i - \sum_{i \in I} s_i \mu_i x_i - \sum_{i \in I} \sum_{j \in J} t_{ij} \lambda_{ij} V_{ij}$$

$$- \sum_{i \in I} \frac{w_i \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \left((\delta_i + \gamma_i)^2 + \delta_i \mu_i \right)}{(\delta_i + \gamma_i) \left(\gamma_i \mu_i - (\delta_i + \gamma_i) \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \right)}$$

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$$\mu_i \geq 0 \quad i \in I$$

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$$\min_{\mu_i} \quad g(\mu_i) = s_i \mu_i + w_i \frac{\tau_i \left((\delta_i + \gamma_i)^2 + \mu_i \delta_i \right)}{(\delta_i + \gamma_i) (\gamma_i (\mu_i - \tau_i) - \tau_i \delta_i)}$$

$$\text{s.t.}$$

$$\mu_i > \tau_i \left(\frac{\delta_i + \gamma_i}{\gamma_i} \right),$$

Solution algorithm



$$\max_{\mathbf{x}, \boldsymbol{\mu}, \mathbf{y}} \quad v(\mathbf{x}, \boldsymbol{\mu}, \mathbf{y}) = \sum_{i \in I} \sum_{j \in J} p_i \lambda_{ij} y_{ij} - \sum_{i \in I} f_i x_i - \sum_{i \in I} s_i \mu_i x_i - \sum_{i \in I} \sum_{j \in J} t_{ij} \lambda_{ij} V_{ij} \\ - \sum_{i \in I} \frac{w_i \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \left((\delta_i + \gamma_i)^2 + \delta_i \mu_i \right)}{(\delta_i + \gamma_i) \left(\gamma_i \mu_i - (\delta_i + \gamma_i) \left(\sum_{j \in J} \lambda_{ij} y_{ij} \right) \right)}$$

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$$\min_{\mu_i} \quad g(\mu_i) = s_i \mu_i + w_i \frac{\tau_i \left((\delta_i + \gamma_i)^2 + \mu_i \delta_i \right)}{(\delta_i + \gamma_i) (\gamma_i (\mu_i - \tau_i) - \tau_i \delta_i)}$$

s.t.

$$\mu_i > \tau_i \left(\frac{\delta_i + \gamma_i}{\gamma_i} \right),$$

$$\mu_i^* = \sqrt{\frac{w_i (\delta_i + \gamma_i)}{s_i \gamma_i} \tau_i + \frac{\delta_i w_i}{s_i \gamma_i^2} \tau_i^2} + \frac{\delta_i + \gamma_i}{\gamma_i} \tau_i.$$

Solution algorithm



$$\max_{\mathbf{x}, \boldsymbol{\mu}, \mathbf{y}} \quad v(\mathbf{x}, \boldsymbol{\mu}, \mathbf{y}) = \sum_{i \in I} \sum_{j \in J} p_i \lambda_{ij} y_{ij} - \sum_{i \in I} f_i x_i - \sum_{i \in I} s_i \mu_i x_i - \sum_{i \in I} \sum_{j \in J} t_{ij} \lambda_{ij} V_{ij}$$

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Solution algorithm



$$\max_{\mathbf{x}, \mathbf{y}} z(\mathbf{x}, \boldsymbol{\mu}^*, \mathbf{y}) = \sum_{i \in I} \sum_{j \in J} A_{ij} y_{ij} - \sum_{i \in I} \sqrt{\sum_{j \in J} B_{ij} y_{ij} + \left(\sum_{j \in J} C_{ij} y_{ij} \right)^2} - \sum_{i \in I} f_i x_i$$

s.t.

$$\sum_{i \in I} y_{ij} \leq 1 \quad j \in J$$
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$$y_{ij} \in \{0,1\} \quad i \in I, j \in J$$
$$x_i \in \{0,1\} \quad i \in I$$

$$A_{ij} = p_i \lambda_{ij} - t_{ij} \lambda_{ij} - \frac{s_i \lambda_{ij} (\delta_i + \gamma_i)^2 + w_i \delta_i \lambda_{ij}}{\gamma_i (\delta_i + \gamma_i)}$$
$$B_{ij} = \frac{4s_i w_i (\delta_i + \gamma_i) \lambda_{ij}}{\gamma_i}$$
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Solution algorithm



$$\max_{\mathbf{x}, \mathbf{y}} z(\mathbf{x}, \boldsymbol{\mu}^*, \mathbf{y}) = \sum_{i \in I} \sum_{j \in J} A_{ij} y_{ij} - \sum_{i \in I} \sqrt{\sum_{j \in J} B_{ij} y_{ij} + \left(\sum_{j \in J} C_{ij} y_{ij} \right)^2} - \sum_{i \in I} f_i x_i$$

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Solution algorithm



$$\max_{\mathbf{x}, \mathbf{y}} \sum_{i \in I} \sum_{j \in J} A_{ij} y_{ij} - \sum_{i \in I} \sqrt{\sum_{j \in J} B_{ij} y_{ij} + \left(\sum_{j \in J} C_{ij} y_{ij} \right)^2} - \sum_{i \in I} f_i x_i + \sum_{j \in J} u_j \left(1 - \sum_{i \in I} y_{ij} \right)$$

s.t.

$$y_{ij} \leq x_i \quad i \in I, j \in J$$

$$y_{ij} \in \{0,1\} \quad i \in I, j \in J$$

$$x_i \in \{0,1\} \quad i \in I$$

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$$B_{ij} = \frac{4s_i w_i (\delta_i + \gamma_i) \lambda_{ij}}{\gamma_i}$$

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Solution algorithm



$$\max_{x,y} \sum_{i \in I} \sum_{j \in J} A_{ij} y_{ij} - \sum_{i \in I} \sqrt{\sum_{j \in J} B_{ij} y_{ij} + \left(\sum_{j \in J} C_{ij} y_{ij} \right)^2} - \sum_{i \in I} f_i x_i + \sum_{j \in J} u_j \left(1 - \sum_{i \in I} y_{ij} \right)$$

s.t.

$$y_{ij} \leq x_i \quad i \in I, j \in J$$

$$y_{ij} \in \{0,1\} \quad i \in I, j \in J$$

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$$B_{ij} = \frac{4s_i w_i (\delta_i + \gamma_i) \lambda_{ij}}{\gamma_i}$$

$$C_{ij} = \frac{2\lambda_{ij}}{\gamma_i} \sqrt{s_i \delta_i w_i},$$

$$\max_{y_{ij} \in \{0,1\}} \sum_{j \in J} D_{ij}^t y_{ij} - \sqrt{\sum_{j \in J} B_{ij} y_{ij} + \left(\sum_{j \in J} C_{ij} y_{ij} \right)^2} - f_i$$

$$D_{ij}^t = p_i \lambda_j - t_{ij} \lambda_j - \frac{s_i \lambda_j (\delta_i + \gamma_i)^2 + w_i \delta_i \lambda_j}{\gamma_i (\delta_i + \gamma_i)} - u_j^t$$

$$B_{ij} = \frac{4s_i w_i (\delta_i + \gamma_i) \lambda_j}{\gamma_i}$$

$$C_{ij} = \frac{2\lambda_j}{\gamma_i} \sqrt{s_i \delta_i w_i},$$

Managerial insights



- Two potential places in each of the five regions are considered for new smelters.
- 90 demand areas for zinc mineralization are indicated.
- The demand rate of area is estimated based on data reported in the NGDI (National Geoscience Database of Iran).
- The transportation cost for each ton is estimated based on data provided by the RMTO (Road Maintenance & Transportation Organization)

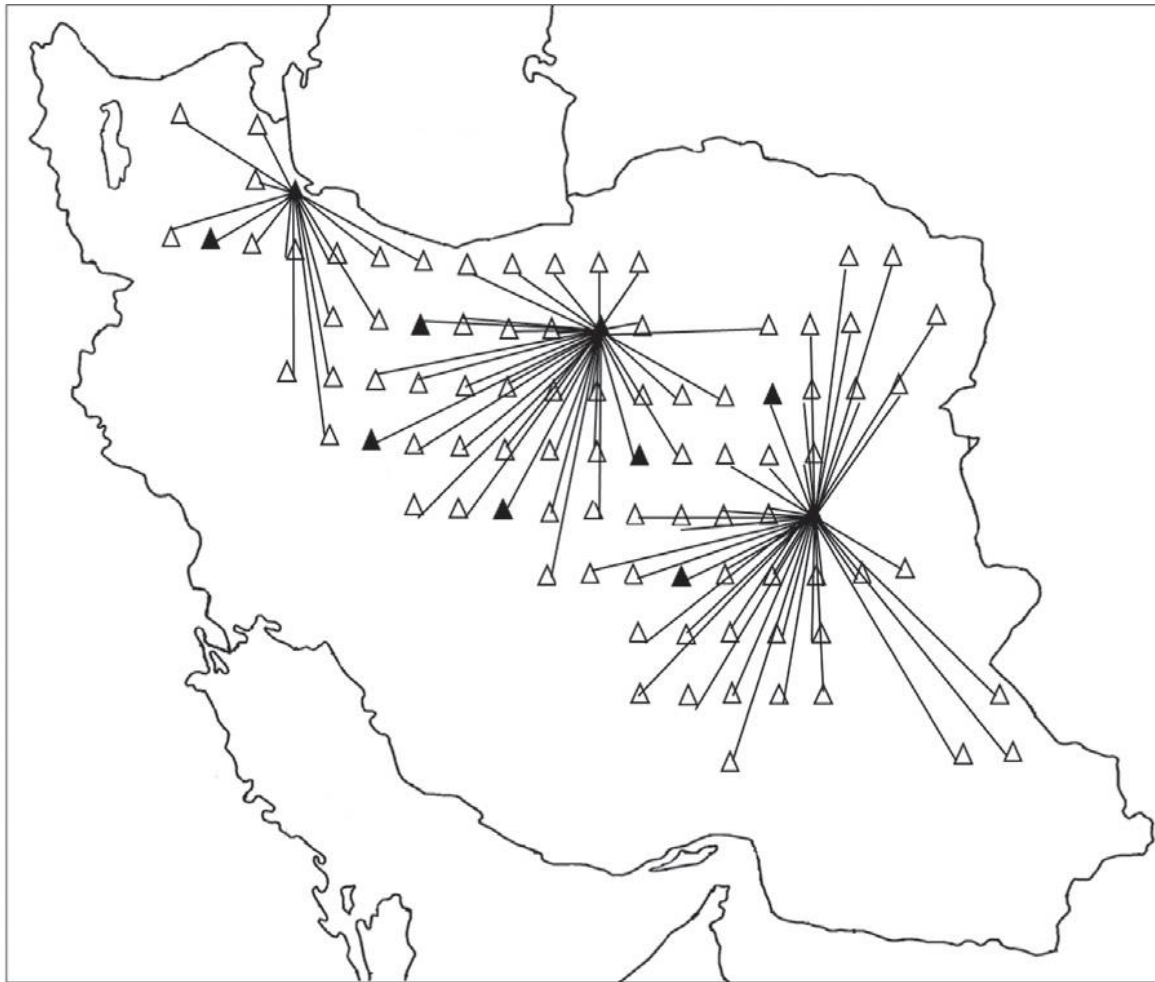
Managerial insights



Case with interruptions

- Expected Total profit:
27 m\$
- Number of Smelters:
2
- Percent of covered deposits:
94%

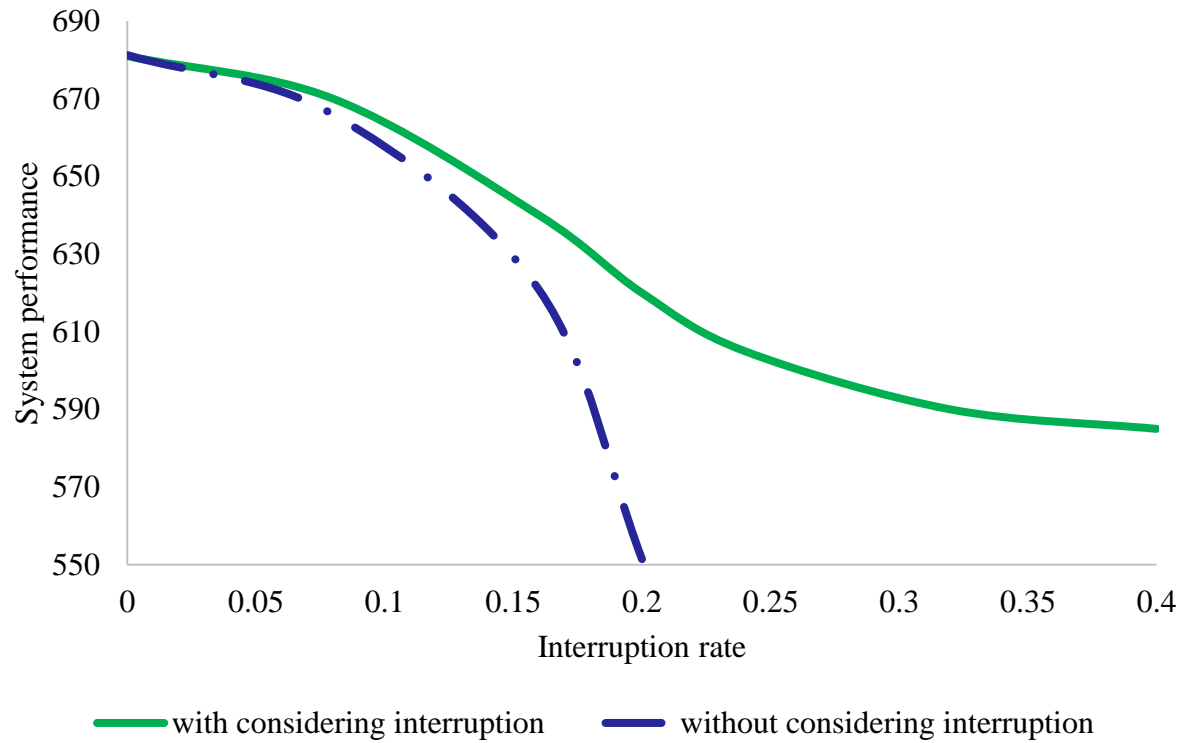
Managerial insights



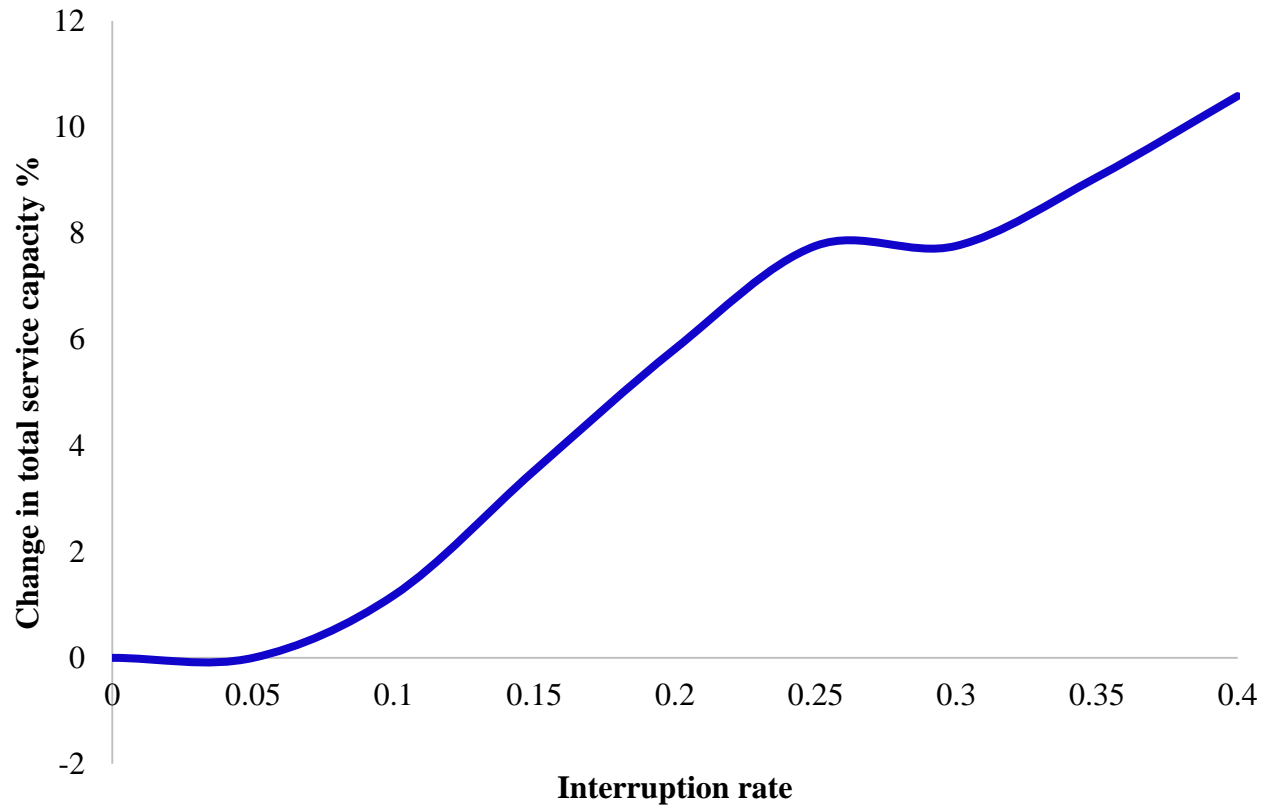
Case without interruptions

- Expected Total profit:
53 m\$
- Number of Smelters:
3
- Percent of covered deposits:
100%

Managerial insights



Managerial insights



Conclusion and extensions



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- Effect of considering service interruption risk on designing an service system is demonstrated.
- Backup service can also be considered as another mitigation strategy along with location-allocation and service capacity ones
- Assessment time is considered before recovery phase.
- The model is extended for other kinds of queue systems in both single server and multiple servers as well as for other kinds of interruptions as well.



Thank you so much for your consideration!